Topics Covered in Math 115

Basic Concepts

Integer Exponents

- Use bases and exponents.
- Evaluate exponential expressions.
- Apply the product, quotient, and power rules.

Polynomial Expressions

- Perform addition and subtraction on monomials.
- Identify the degree and leading coefficient of a polynomial.
- Perform addition and subtraction on polynomials.
- Find the opposite of a polynomial.
- Apply the distributive property.
- Perform multiplication on polynomials.
- Find the product of a sum and difference.
- Square a binomial.

Factoring Polynomials

- Factor out the greatest common factor.
- Factor by grouping.
- Factor trinomials with a leading coefficient of 1.
- Factor trinomials by grouping (AC method).
- Factor trinomials using FOIL (trial-and-error).
- Factor trinomials with a greatest common factor.
- Factor the difference of two squares.
- Factor perfect square trinomials.
- Factor an expression completely.

Radical Notation / Radical Expressions

• Instruction/exercises sufficient to enable student to simplify square roots in quadratic formula and perform necessary operations in exponential and logarithmic equations.

Introduction to Functions and Graphs

Numbers, Data, and Problem Solving

- Recognize common sets of numbers.
- Evaluate expressions by applying the order of operations.
- Learn scientific notation and use it in applications.*
- Apply problem-solving strategies.

Visualizing and Graphing Data

- Analyze one-variable data.
- Find the domain and range of a relation.
- Graph in the xy-plane.

- Calculate distance.
- Use the midpoint formula.
- Learn to graph with a calculator.

Functions and Their Representations

- Learn function notation.
- Graph functions by plotting points.
- Identify the domain and range of a function.
- Use a calculator to represent functions.
- Represent a function four different ways.
- Determine if a relation is a function.
- Solve applications.*

Types of Functions

- Find the slope and b for a linear function.
- Find and interpret slope as a rate of change.
- Determine if a function is linear or nonlinear and graph.
- Determine if data is linear or nonlinear and graph or identify the slope.
- Sketch a curve that satisfies a verbal description.

Functions and Their Rates of Change

- Identify where a function is increasing or decreasing.
- Use interval notation.
- Use and interpret average rate of change.

Linear Functions and Equations

Linear Functions and Models

- Find the average rate of change.
- Determine whether a function models the data exactly or approximately.
- Analyze and graph linear functions.
- Model data with a linear function.
- Evaluate and graph piecewise-defined functions.
- Use linear regression to model data.

Equations of Lines

- Find the point-slope form of a line.
- Find the slope-intercept form of a line.
- Write equations for horizontal, vertical, parallel, and perpendicular lines.
- Find the intercepts of a line.
- Apply interpolation and extrapolation.
- Solve applications.*
- Use direct variation to solve problems.

Linear Equations

- Use concepts about linear equations.
- Identify linear and nonlinear equations.
- Solve linear equations symbolically.
- Solve linear equations graphically.
- Solve linear equations numerically.
- Solve equations for a variable.
- Solve applications.*
- Find a linear function that models the data.

Linear Inequalities

- Express an inequality in interval notation.
- Solve linear inequalities symbolically.
- Solve linear inequalities graphically.
- Solve linear inequalities numerically.
- Solve compound inequalities.
- Solve applications.*

Absolute Value Equations and Inequalities

- Evaluate and graph the absolute value function.
- Solve absolute value equations.
- Solve absolute value inequalities.
- Solve applications.*

Quadratic Functions and Equations

Quadratic Functions and Models

- Learn basic concepts about quadratic functions and their graphs.
- Apply the vertex formula.
- Graph a quadratic equation by hand.
- Solve applications and model data.
- Use quadratic regression to model data.

Quadratic Equations and Problem Solving

- Find the domain of a function.
- Solve quadratic equations.
- Solve problems involving quadratic equations.
- Solve an equation for a variable.

Quadratic Inequalities

- Solve quadratic inequalities graphically.
- Solve quadratic inequalities symbolically.
- Solve applications.*

Exponential and Logarithmic Functions

Combining Functions

- Perform arithmetic operations on functions.
- Review function notation.
- Perform composition of functions.
- Solve applications.*

Inverse Functions and Their Representations

- Calculate inverse operations.
- Identify one-to-one functions.
- Find inverse functions symbolically.
- Use other representations to find inverse functions.
- Solve applications.*

Exponential Functions and Models

- Evaluate exponential expressions.
- Distinguish between linear and exponential growth.
- Calculate compound interest.
- Graph and model data with exponential functions.
- Solve applications.*

Logarithmic Functions and Models

- Evaluate the common logarithm function.
- Find the domain of a logarithmic function.
- Evaluate logarithms with other bases.
- Solve exponential equations.
- Solve logarithmic equations.
- Graph logarithmic functions.
- Convert between exponential and logarithmic forms.
- Solve applications.*

Properties of Logarithms

- Apply basic properties of logarithms.
- Expand and combine logarithmic expressions.
- Graph logarithmic functions.
- Use the change of base formula.
- Solve applications.*

Exponential and Logarithmic Equations

- Solve exponential equations.
- Solve logarithmic equations.
- Solve applications.*

Constructing Nonlinear Models

- Select and find an appropriate model.
- Use exponential and logarithmic regression to model data.
- Solve applications.*

Systems of Equations and Inequalities

Functions and Systems of Equations in Two Variables

- Evaluate functions of two variables.
- Understand basic concepts about systems of equations.
- Recognize types of linear systems.
- Apply the method of substitution.
- Apply the elimination method.
- Apply graphical and numerical methods.
- Solve applications.*

^{*} Applications chosen should be non-STEM to the maximum extent possible.